

Quiz 3

STAT 381, APPLIED STATISTICAL METHODS I, SPRING 2015

NAME: *Solutions*

Problem 1. Random variable X can take values 0, 1, or 2 with positive probability. Its pmf is $f(x) = c(3+x)$.

a. (3 points) Find the constant c .

$$f(0) + f(1) + f(2) = 1$$

$$\text{LHS} = c(3+0) + c(3+1) + c(3+2) = c(12) = 1 \Rightarrow c = \frac{1}{12}$$

b. (2 points) Find $P(-1 \leq X \leq 1)$.

$$P(-1 \leq X \leq 1) = P(X=0 \text{ or } X=1)$$

$$= f(0) + f(1)$$

$$= \frac{1}{12}(3) + \frac{1}{12}(4) = \frac{7}{12}$$

Problem 2. Random variable Y has support $[0, 3]$. Its pdf is $f(y) = k(3-y)$.

a. (3 points) Find the constant k .

$$\int_0^3 k(3-y) dy = k \left[3y - \frac{1}{2}y^2 \right]_0^3 = k \left[9 - \frac{9}{2} \right] = \frac{9}{2}k = 1$$

$$\Rightarrow k = \frac{2}{9}$$

b. (2 points) Find $P(-1 \leq Y \leq 1)$.

$$P(-1 \leq Y \leq 1) = P(0 \leq Y \leq 1) = \int_0^1 \frac{2}{9}(3-y) dy$$

$$= \frac{2}{9} \left[3y - \frac{1}{2}y^2 \right]_0^1 = \frac{2}{9} \left[\frac{5}{2} \right]$$

$$\frac{5}{9}$$