

**True/False Tailgate**

*Defend your responses*

1.  $\lim_{(x,y) \rightarrow (0,0)} \frac{\sin(y)}{x} = 0$
2. The directional derivative of a function  $f$  in a direction  $u$ , where  $\|u\| = 1$  is defined  $D_u f = u \cdot \nabla f$ .
3. The equation  $\phi = \pi/4$  (in spherical coordinates) describes a plane.
4. The equation  $\theta = \pi/4$  (in spherical or polar coordinates) describes a plane.
5. If  $F(x, y, z) = 0$ , then  $\frac{\partial x}{\partial y} \frac{\partial y}{\partial z} \frac{\partial z}{\partial x} = -1$ .
6. All differentiable functions are continuous.
7. If the gradient of a function exists then it is differentiable.
8. Areas of regions are preserved by the transformation  $x = 2u + v$ ,  $y = 3u + 2v$ .
9. The tangent plane to  $z = x^2 - y^2$  at  $(1, 1, 0)$  is horizontal.
10.  $\int_0^1 \int_{x^4}^{x^2} xy^2 dy dx = \int_0^1 \int_{y^{1/4}}^{y^{1/2}} xy^2 dx dy$

**Bears Problems**

*Not just the lack of Urlacher*

1. Soldier field, at first approximation, can be described by the region between  $z = \frac{1}{3}(x^2 + y^2)$ ,  $x^2 + y^2 + z^2 = 4$ , and above  $z = 0$ . Find the volume of the stadium using these surfaces. *Hint, use cylindrical polar coordinates.*
2. What units would make this number a decent approximation?  
*This would never be on the exam, but google asks this type of question to their job applicants.*