

November 11

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1. Evaluate the following limits

(a) $\lim_{x \rightarrow e} \frac{\ln x - 1}{x - e}$

(b) $\lim_{u \rightarrow \pi/4} \frac{\tan u - \cot u}{u - \pi/4}$

(c) $\lim_{x \rightarrow \infty} \frac{3x^4 - x^2}{6x^4 + 12}$

(d) $\lim_{x \rightarrow \pi/2} \frac{2 \tan x}{\sec^2 x}$

(e) $\lim_{x \rightarrow 0} x \csc x$

(f) $\lim_{x \rightarrow \infty} x - \sqrt{x^2 - 1}$

(g) $\lim_{x \rightarrow 0^+} x^{2x}$

(h) $\lim_{x \rightarrow 0} (1 + 4x)^{3/x}$

(i) $\lim_{\theta \rightarrow \pi/2^-} (\tan \theta)^{\cos \theta}$

2. Compare the growth rates of the following functions

(a) $x^{10}; e^{0.01x}$

(b) $\ln \sqrt{x}; \ln^2 x$

3. Evaluate this limit, which appeared in L'Hôpital's book.

$$\lim_{x \rightarrow a} \frac{\sqrt{2a^3x - x^4} - a\sqrt[3]{a^2x}}{a - \sqrt[4]{ax^3}}$$

4. Consider the following limit

$$\lim_{x \rightarrow \infty} \frac{\sqrt{ax + b}}{\sqrt{cx + d}}$$

where a, b, c, d are all positive real numbers. What happens when L'Hôpital's rule is used? How else can the limit be found?

5. Find all antiderivatives

(a) $g(x) = 11x^{10}$

(b) $f(x) = -4 \cos(4x)$

(c) $f(y) = \frac{-2}{y^3}$

6. Solve the indefinite integrals

(a) $\int (3x^5 - 5x^9) dx$

(b) $\int (\sec^2 - 1) dx$

(c) $\int \frac{3}{4+v^2} dx$

7. Solve for the antiderivative using the initial conditions

(a) $f(t) = \sec^2 t, F(\pi/4) = 1$

(b) $g'(x) = 7x(x^6 - \frac{1}{x}), g(1) = 24$

(c) $F''(x) = \cos x, F'(0) = 3, F(\pi) = 4$