

Quiz 7

STAT 381, APPLIED STATISTICAL METHODS I, SPRING 2015

NAME:

Problem 1. (5 points) At an order fulfillment center it takes on average 5 minutes to complete an order with a standard deviation of 2 minutes. 65 orders have to be completed, what is the probability it will take less than 5 hours?

$$S_{65} \sim N(325, 65 \cdot 2^2)$$

$$\uparrow$$

$$6.38 \cdot 16.125^2 \quad z = \frac{300 - 325}{16.125}$$

$$P(S_{65} < 300) = P(Z < -1.55) = .0606$$

Problem 2. (5 points) Two independent random samples of sizes 33 and 45 are drawn from a population with $\mu = 7$ and $\sigma = 3$. What is the probability that the absolute difference of sample means is greater than 1, i.e. what is $P(|\bar{X}_1 - \bar{X}_2| > 1)$?

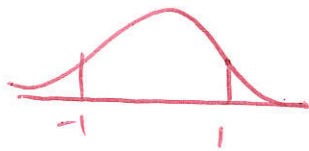
$$\bar{X}_1 - \bar{X}_2 \sim N(\mu_1 - \mu_2, \frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2})$$

$$\equiv N(0, \frac{9}{33} + \frac{9}{45}) \equiv N(0, .688^2)$$

$$z = \frac{-1 - 0}{.688} = -1.45$$

$$P(|\bar{X}_1 - \bar{X}_2| > 1) = 2P(\bar{X}_1 - \bar{X}_2 < -1) = 2P(Z < -1.45)$$

$$= 2(.0735)$$



$$= .147$$

Bonus (3 points) If X follows a Gamma distribution with $\alpha = 50, \beta = 3$, what precise distribution could we use to approximate X , justified by the Central Limit Theorem?

$$E(X) = 50 \cdot 3 = 150$$

$$\text{Var}(X) = 50 \cdot 3^2 = 450$$

since $n > 30$, X can be approximated by $N(\mu=150, \sigma^2=450)$

as X can be thought of

a sum of 50 indep $\text{exp}(3)$ random variables.