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Show all work. Unjustified answer yields no credit.

Decide if each set is a basis in the corresponding vector space.

a. $(1, 2)^T, (1, 0)^T, (0, 1)^T$ in \mathbb{R}^2 .

b. $x^3 + 2x^2 + 3x + 4, 2x^3 + 3x^2 + 4x + 5, 3x^3 + x - 2$ in P_3 .

c. $(1, 1, -1)^T, (2, 1, 0)^T, (3, 2, 1)^T$ in \mathbb{R}^3 .

2 a. Not in \mathbb{R}^2 number of vector in a basis is 2

2 b. Not in P_3 number of vectors in a basis is 4

c. $R_2 - R_1 \rightarrow R_3 + R_1 \rightarrow \begin{bmatrix} 1 & 2 & 3 \\ 1 & 1 & 2 \\ -1 & 0 & 1 \end{bmatrix} \xrightarrow{2} \begin{bmatrix} 1 & 2 & 3 \\ 0 & -1 & -1 \\ 0 & 2 & 4 \end{bmatrix} \xrightarrow{\substack{-R_2 \rightarrow R_2 \\ R_3 - 2R_2}} \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 1 \\ 0 & 2 & 4 \end{bmatrix} \sim$

$\frac{1}{2}R_3 \rightarrow R_3 \rightarrow \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 1 \\ 0 & 0 & 2 \end{bmatrix} \sim \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} \quad \text{rank } A = 3$

So the three column are lin. ind. Hence the original 3 vectors form a basis in \mathbb{R}^3 . 2