

Questions are numbered as in Gallian, pp. 23–24.

2. Determine $\gcd(2^4 \cdot 3^2 \cdot 5 \cdot 7^2, 2 \cdot 3^3 \cdot 7 \cdot 11)$ and $\text{lcm}(2^3 \cdot 3^2 \cdot 5, 2 \cdot 3^3 \cdot 7 \cdot 11)$.
8. Suppose a and b are integers that divide the integer c . If a and b are relatively prime, show that ab divides c . Show, by example, that if a and b are not relatively prime, then ab need not divide c .
12. Let a and b be positive integers, and let $d = \gcd(a, b)$ and $m = \text{lcm}(a, b)$. If t divides both a and b , prove that t divides d . If s is a multiple of both a and b , prove that s is a multiple of m .
16. Use the Euclidean algorithm to find $\gcd(34, 126)$ and write it as a linear combination of 34 and 126.
22. Prove that $2^n 3^{2n} - 1$ is always divisible by 17.