Directions: Answer all questions and show all work in the **exam book-let** provided. Start each new question at the **top** of a new page and **box** your final answer. Questions 2 - 4, 6 are worth 15 points, Questions 1 and 5 are 20 points.

- 1. (a) Find the general solution of: 4y'' 4y' + y = 0
 - (b) Find the general solution of: y'' + 2y' + 2y = 0
 - (c) The functions x^2 and 1/x are solutions to a 2nd order, linear homogeneous ODE on x > 0. Verify whether or not the two solutions form a fundamental solution set.
- 2. Solve the IVP:

$$y\frac{dy}{dx} = \frac{3x^2 + 4x + 2}{2y + 1}, \quad y(0) = -1$$

3. Solve the IVP:

$$\frac{dy}{dt} + 4y = e^{-t}, \quad y(0) = 4/3$$

4. Find the general solution of

$$y''(x) + 4y'(x) + 4y = e^{-2x}\ln(x) + 8$$

- 5. A large tank is initially empty. At time t = 0, a brine solution begins to enter the tank at the rate of 6 L/min with concentration 2 Kg/L. The well-stirred solution is removed from the tank at the rate of 5 L/min. State and solve for A(t) = the amount of salt in the tank at time t.
- 6. Consider $y' = -xy + y^2$, y(0) = 1
 - (a) Approximate y(1/10) using Euler's method with step size h = 1/10.
 - (b) Approximate y(1/10) using Improved Euler's method with step size h = 1/10. Use part (a) as your prediction step.