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   - elements and behavior
   - executing programs

2. Python Programming
   - developing programs
   - use as a calculator
   - converting strings to numbers

3. Summary + Assignments
Machine Architecture
using Python as a calculator

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John von Neumann
first computer of the Institute for Advanced Study

http://www-groups.dcs.st-and.ac.uk/~history/Mathematicians/Von_Neumann.html
Elements of the Machine
five components

The main components of a computer are
1. processor (or CPU) for control and execution;
2. memory (or RAM) to store programs and data;
3. storage for keeping permanent data;
4. peripherals to communicate with the computer;
5. system bus for connecting all components.

The processor **fetches** instructions from memory, **decodes** them, and **executes**: the von Neumann machine.

The stages of the processor are synchronized by the **system clock**. The frequency of the clock (#ticks per second) gives an upper bound on #arithmetical operations per second the computer can perform.
In a computer all information is encoded in binary form.

- The binary number system uses bits \( \in \{0, 1\} \).

- Eight bits form a **byte**: 
  - with 8 bits we have \( 2^8 \) numbers, from 0 to 255;
  - a byte is also called a **word**, fits in 1 memory cell.

- The ASCII (American Standard Code for Information Interchange) code uses 7 bits for 128 characters. Often the code is extended to 8 bits.

- A more extensive code is Unicode: 
  - 16 bits, for \( 2^{16} = 65,536 \) different bit patterns, to represent text in languages as Chinese.
The processor consists of the following units:

1. The **control unit** fetches and decodes instructions. It also sends control signals.

2. The **system clock** synchronizes operations.

3. The **arithmetic and logic unit (ALU)** performs the operations.

The CPU has several *registers*. A register is a memory cell which can be accessed very quickly.
The Principal CPU Registers

All data handled by the processor is held in registers. The principal registers are

1. data registers and address registers
2. current instruction register
3. program counter
4. interrupt register
5. registers which contain operands
6. several working registers

The ALU (Arithmetic and Logic Unit) also uses registers. One particular register is the status register which carries in its bits information about the results of an operation.
2. Main Memory
RAM and ROM

- RAM = Random Access Memory, available to user;
  ROM = Read Only Memory, used to store microprograms
delivered by the manufacturer.

- The main memory is a sequence of memory cells.
The size of one memory cell is one or several bytes.

- Every memory cell has an address. Memory addressing happens
  via an address register.
  An address register of $k$ bits reaches $2^k$ cells.
  A 32-bit address register means that 4Gb of RAM can be
  addressed; 64-bit memory architectures can address 16 exabytes.

- Between the registers and main memory: cache.
3. Mass Storage
to store permanently

Older technology includes tapes and floppy disks. We distinguish between removable and hard drives:

1. the hard drive, the disk inside the computer;
2. USB memory keys act as hard drives, but portable;
3. CD-ROM = Compact Disc Read Only Memory
   DVD = Digital Versatile Disc

The organization of information is often as a tree
- a file stores a program or data;
- a directory contains several files.
4. Input/Output Interfaces

to connect to peripherals

Input/Output interfaces form the circuitry to connect the computer with the peripherals.

An interface typically contains the following elements:

1. a peripheral data register
2. a peripheral command register
3. status information about the peripheral

Some of these interfaces have grown very intelligent, i.e.: video cards have become complex and powerful. The success of the gaming industry led to the cell processor.

Graphics card have a theoretical performance of a trillion floating point operations per second and have surpassed CPUs in performance.
5. System Bus
for connecting components

The processor activates other units via the system bus.

Data is divided in three categories:

- **data bus** transfers data from memory into data register and vice versa;

- **address bus** transmits contents of address register to main memory;

- **control bus** transfers instructions to be executed.
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Executing Programs

imagine what your program does

Consider the python command print ’hello world’.

The following tasks need to happen:
1. fetch the instruction
2. decode the instruction as a print
3. get the argument of the print
4. pass the command to the screen device

Each of this four steps involves many more steps...
Assembly Language

Machine instructions are sequences of bits.

Some terminology:

- An assembly language is a mnemonic system for representing machine instructions.
- An assembler is a program to translate assembly language into machine instructions.

Writing assembly language has some advantages:

1. develop good understanding of how it really works
2. the resulting code can be very efficient

Drawbacks of programming in assembly language:

1. requires a very disciplined style of coding
2. assembler language depends on the architecture and the code is often not portable
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Developing Python programs

Use python interactively, or run \texttt{m.py} as \texttt{python m.py}.

As Python is interpreted, use incremental development:
1. first try the commands in an interactive session
2. save the working commands in a file (e.g. as \texttt{w.py})
3. test the program, run as \texttt{python w.py}
4. if the run fails, retry the commands interactively
5. after success, continue step 1 with new commands

Save intermediate versions of \texttt{working} programs.
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- Type expressions at the python prompt operations: +, −, *, /, and exponentation **.

- Long integers and floats

>>> (2**10)**10
1267650600228229401496703205376
>>> (2.0**10)**10
1.2676506002282294e+30

Floats are limited in size, long integers are not.

- store results with the assignment

>>> x = 2**10
>>> x**10

useful to control the order of calculations.
Names of variables are case sensitive.
The machine precision $\varepsilon$ is the largest number that when added to 1.0 results in a number different from 1.0.

Determine $\varepsilon$ experimentally in the Python shell

```python
>>> 1.0 + 2**(-52)
1.0000000000000002
>>> 1.0 + 2**(-53)
1.0
```

In double floating-point precision, we have $\varepsilon = 2^{-52}$.

The $\varepsilon$ (also called machine epsilon) gives an upper bound for the largest roundoff error in a floating-point operation.
computing with fractions

In the example session below we import everything from fractions:

```python
>>> from fractions import *
>>> a = Fraction(3,4)
>>> a
Fraction(3, 4)
>>> a.numerator
3
>>> a.denominator
4
>>> b = Fraction(5,6)
>>> a + b
Fraction(19, 12)
>>> gcd(4,6)
>>> gcd(4,6)
2
```

Thanks to this import we also could compute a greatest common divisor with the `gcd` function of the `fractions` module.
online help

```python
>>> help('**')
displays help on power operator

>>> help('OPERATORS')
gives overview of operators

ˆ is bitwise XOR operator

2**7 ≠ 2 ^ 7
Versions of Python divide

Versions 3.0 and higher of Python use `//` for the integer division operator.

<table>
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<th>version</th>
<th>Python Version</th>
<th>result</th>
</tr>
</thead>
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<td>7/2</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>7//2</td>
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<tr>
<td>float division</td>
<td>7.0/2</td>
<td>3.5</td>
</tr>
<tr>
<td></td>
<td>7/2</td>
<td></td>
</tr>
</tbody>
</table>
ASCII Codes in Python

The function `ord` returns the ASCII code of a character:

```python
>>> ord('a')
97
>>> ord('1')
49
>>> ord('?')
63
>>> 'a' > '?'
True
```

The function `chr` returns the character with given order:

```python
>>> chr(98)
'b'
```
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Converting Strings to Numbers (after input())

The result of `input()` is a string.

If this string represents a number, before we can calculate with it, we must convert it to a number type, e.g.: `float`.

```python
>>> n = input('give a number: ') 
give a number: 3.4
>>> type(n)
<class 'str'>
>>> fn = float(n)
>>> type(fn)
<class 'float'>
>>> fn
3.4
```

Every Object in Python has a Type!
Converting Numbers to Strings (formatting operator)

Sometimes only few decimal places of a floating-point number are needed for display.

Use of the % Operator:

```python
>>> x = 1.238
>>> sx = '%.2f' % x
>>> print(sx)
1.24
```

Types of the variables `x` and `sx` are different:

```python
>>> type(x)
<type 'float'>
>>> type(sx)
<type 'str'>
```
the functions `hex()`, `bin()`, and `int()`

```python
>>> n = 123
>>> hn = hex(n)
>>> hn
'0x7b'

With `hex()`, we verified that $123_{10} = 7b_{16}$. Now in reverse:

```python
>>> int(hn, base=16)
123
```

With `bin()`, we check that $123_{10} = 111\ 1011_2$:

```python
>>> bn = bin(n)
>>> bn
'0b1111011'
>>> int(bn, base=2)
123
```
Summary + Assignments

Background:
- chapter 2 of *Computer Science. An Overview*; and
- topics of chapter 1 of *Python Programming in Context*.

Assignments:
1. Suppose two numbers are in main memory. Describe the fetch-decode-execute cycle to compute their sum and place the sum in main memory.
2. Explain the outcome of $2 \wedge 7$.
3. Compute $\frac{1}{3}$ and $\frac{1}{3}$ in Python. Explain why the answers are so different.
4. Represent the string `hello` as a string of bits, replacing each character by its ASCII code. Give the hexadecimal representation of the bit string.