

# Outline

## 1 Digital Systems

- transistors
- logic gates

## 2 Dictionaries and Conditional Statements

- intrinsic operations
- writing numbers in words

MCS 260 Lecture 9  
Introduction to Computer Science  
Jan Verschelde, 23 June 2023

# Digital Systems

## introduction to electronic circuits

A computer is a synchronous binary digital system.

**digital:** all information is discrete (not continuous)

**binary:** only zero and one are used  
a binary digit is a bit

**synchronous:** functioning is ruled by the system clock

Basic elements to represent bits are switches that can be open (1) or closed (0).

Transistors are electronic circuits to represent bits.

# transistors and gates

## intrinsic operations

### 1 Digital Systems

- **transistors**
- logic gates

### 2 Dictionaries and Conditional Statements

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# Transistors

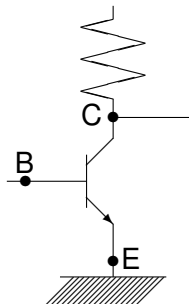
electronic circuits to represent bits

Transistors have three connections to the outside:

- 1 base: input voltage
- 2 collector: output voltage
- 3 emitter: to ground

High Voltage: 1

Low Voltage: 0



# transistors and gates

## intrinsic operations

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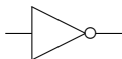
# Logic Gates

implement logic operators

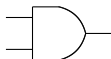
Logic gates are circuits that correspond to logic operators.

Representations of NOT, AND, OR:

NOT



AND



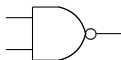
OR



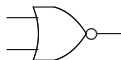
$x \text{ NAND } y$   
 $= \text{NOT } (x \text{ AND } y)$

$x \text{ NOR } y$   
 $= \text{NOT } (x \text{ OR } y)$

NAND

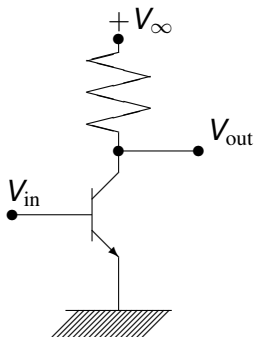


NOR



# A NOT Gate

as realized by a transistor



Input Voltage  $V_{in}$

$V_{in} = \text{low}$

$\Rightarrow$  switch is open

$\Rightarrow V_{out} = +V_{\infty}$

$V_{in} = \text{high}$

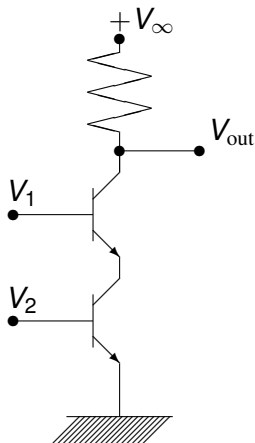
$\Rightarrow$  switch is closed

$\Rightarrow V_{out} = \text{low}$

A NOT gate converts a low input voltage to high and a high input voltage to low.

# A NAND Gate

two transistors in series



Input voltages  $V_1$  and  $V_2$

If either  $V_1$  or  $V_2$  is low:

$\Rightarrow$  switch is open

$\Rightarrow V_{out} = +V_{\infty}$

If both  $V_1$  and  $V_2$  are high:

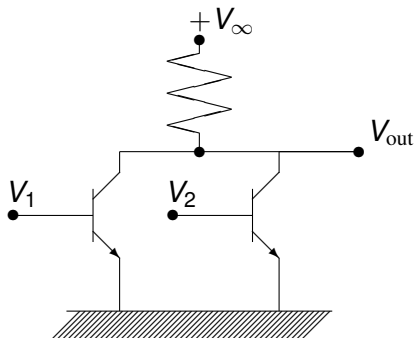
$\Rightarrow$  switch is closed

$\Rightarrow V_{out} = \text{low}$



# A NOR Gate

two transistors in parallel



Input voltages  $V_1$  and  $V_2$

if either  $V_1$  or  $V_2$  is high  $\Rightarrow$  closed switch  $\Rightarrow V_{out} = \text{low}$ ;

if both  $V_1$  or  $V_2$  are low  $\Rightarrow$  open switch  $\Rightarrow V_{out} = +V_{\infty}$ .

# transistors and gates

## intrinsic operations

### 1 Digital Systems

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### 2 Dictionaries and Conditional Statements

- **intrinsic operations**
- writing numbers in words

## intrinsic operations

Intrinsic operations are those operations that belong to the standard library.

For every variable  $x$ , the function

`id(x)` returns the address of  $x$ ,

`type(x)` returns the type of  $x$ .

Python has dynamic typing and garbage collection.

To see the operations defined on strings, do

```
>>> dir(str)
```

which returns the list of operations defined on strings. Then,

```
>>> help(str.split)
```

shows the help on the `split()` method on strings.

# transistors and gates

## intrinsic operations

### 1 Digital Systems

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## writing numbers in words – applying dictionaries

On a check, the amount is spelled out in words.

Program specification:   Input:  $n$ , a natural number  $< 1000$ .  
                              Output: a string expressing  $n$  in words.

An example session with `write_numbers.py`:

```
$ python write_numbers.py  
give a natural number : 125  
125 is one hundred and twenty five
```

# the dictionary: numbers spelled out in English

For all  $n \leq 20$  and multiples of 10:

```
DIC = { \
  0:'zero', 1:'one', 2:'two', 3:'three', \
  4:'four', 5:'five', 6:'six', 7:'seven', \
  8:'eight', 9:'nine', 10:'ten', \
  11:'eleven', 12:'twelve', 13:'thirteen', \
  14:'fourteen', 15:'fifteen', 16:'sixteen', \
  17:'seventeen', 18:'eighteen', 19:'nineteen', \
  20:'twenty', 30:'thirty', 40:'forty', \
  50:'fifty', 60:'sixty', 70:'seventy', \
  80:'eighty', 90:'ninety', 100:'hundred' \
}
```

The dictionary lookup `DIC[n]` handles special cases.

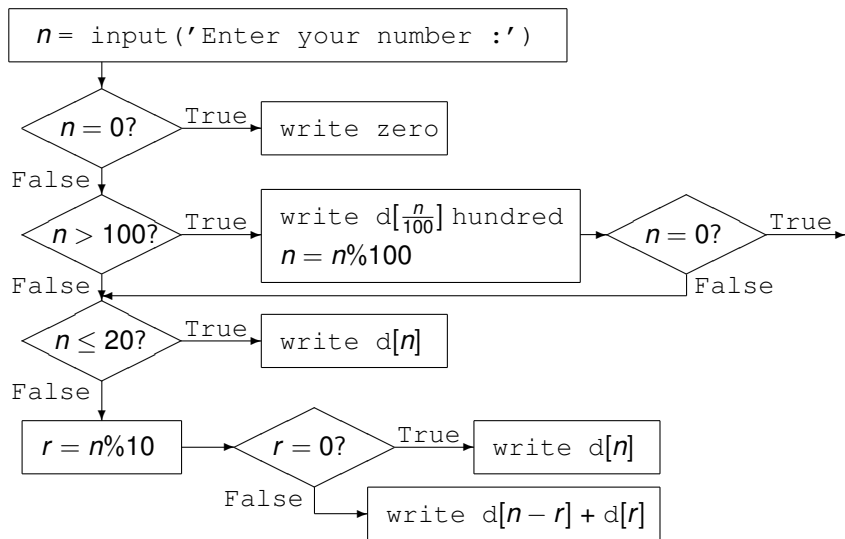
# idea for the algorithm

## case analysis

We distinguish three cases:

- 1 the trivial case:  $n = 0$   
This is the only case we write `zero`.
- 2 large numbers  $n \geq 100$   
We start writing  $n/100$  `hundred`  
and then continue with
- 3 the rest:  $0 < n < 100$ :
  - 1 for  $n \leq 20$ : dictionary lookup
  - 2 for  $20 < n < 100$ : compute  $r = n\%10$  and  $n - r$

# flowchart for `write_numbers.py`





# Exercises

- 1 Draw all transistors needed to realize an OR gate and describe its working.
- 2 Construct truth tables for
  - 1  $(A \text{ OR } B) \text{ OR NOT } (A \text{ AND } B)$
  - 2  $\text{NOT } ((A \text{ OR } C) \text{ OR } B) \text{ OR } (A \text{ AND } C)$
- 3 Draw the logic gates to realize the expressions of the previous exercise.
- 4 Let `secret` be a secret number the user of a Python program has to guess. Give code for prompting the user for a guess and for printing feedback.
- 5 Write a script to use `dbm` to store the dictionary `d` to spell numbers out in English.
- 6 Modify the `write_numbers.py` program so it uses the `dbm` file made in the previous exercise.