

# Three Dimensional Plots

## 1 Surfaces

- the graph of a function
- equations in three variables
- surfaces in parameter form

## 2 Space Curves

- defined in parameter form
- as the intersection of two surfaces

## 3 Four Dimensional Plots

- a Riemann surface

MCS 320 Lecture 27  
Introduction to Symbolic Computation  
Jan Verschelde, 12 July 2024

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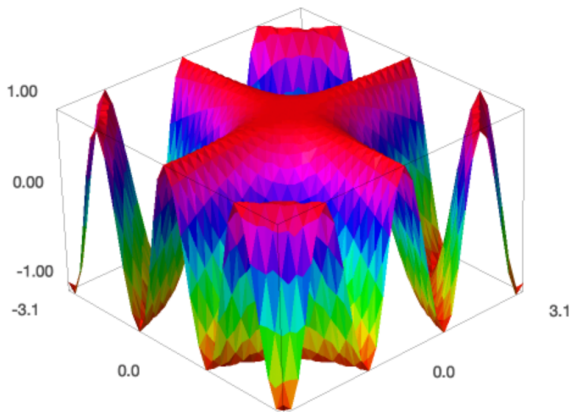
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# the Graph of a Function $z = \cos(x \cdot y)$



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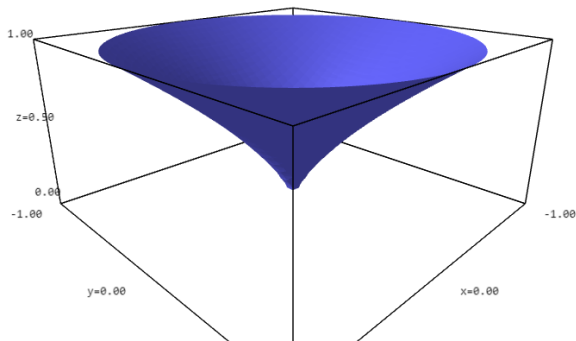
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# A Surface Implicitly Defined by $z^3 - x^2 - y^2 = 0$



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# Three Functions in Two Variables

$$(x = x(u, v), y = y(u, v), z = z(u, v))$$



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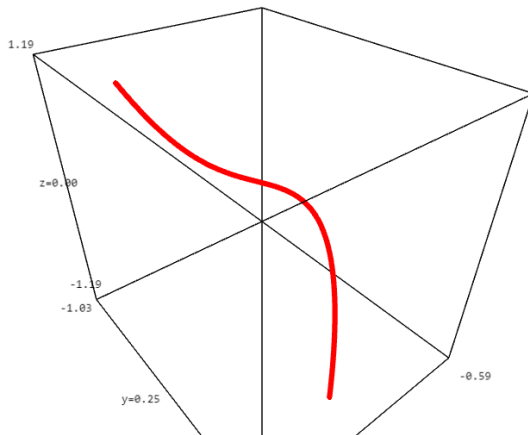
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## parameter form $(x(t), y(t), z(t))$

The twisted cubic is defined by  $(t, t^2, t^3)$ .



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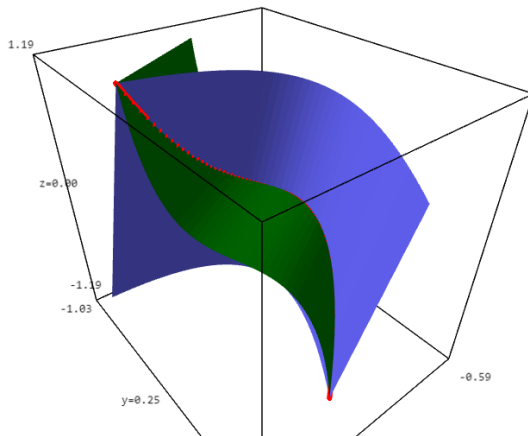
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# The Intersection of Two Cylinders

The twisted cubic is defined by  $x^2 - y = 0$ ,  $x^3 - z = 0$ .



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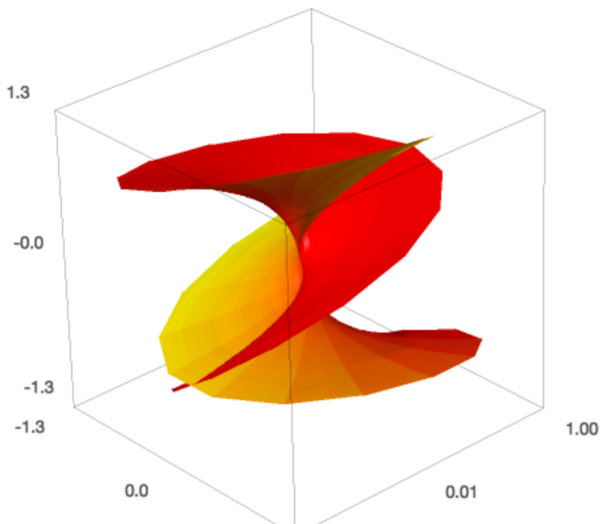
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# A Riemann Surface of $z = w^3$ , $w = u + v\sqrt{-1}$



$z = x + y\sqrt{-1}$ , the height of the surface is  $u$ , its color is  $v$ .