

# Massaging a picture

CTTI

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**Lemma 0.1.** *If two rectangles  $ABGE$  and  $WXYZ$  have equal content there is a rectangles  $ACID$ , with the same content as  $WXYZ$  and satisfying the following diagram. Further the diagonals of  $AF$  and  $FH$  are collinear.*

{areadiag}

Proof. Suppose  $AB$  is less than  $WX$  and  $YZ$  is less than  $AE$ . Then make a copy of  $WXYZ$  as  $ACID$  below. The two triangles are congruent. Let  $F$  be the intersection of  $BG$  and  $DI$ . Construct  $H$  as the intersection of  $EG$  extended and  $IC$  extended.

Now, prove  $F$  lies on  $AH$ .

