

1. (Redux) Consider  $f(x) = x^2 + 1$  on the interval  $[0, 4]$ . Let  $n = 4$ .

- (a) Sketch the graph of  $f(x)$ .
  - (b) Divide the interval into  $n = 4$  equal subintervals. What is the length of each subinterval?
  - (c) Indicate the endpoints of each subinterval on your graph from part (a).
  - (d) Draw the rectangles corresponding to the left Riemann sum for  $n = 4$ .
  - (e) On the same graph, draw the rectangles for the right Riemann sum.
  - (f) Compute the left and right Riemann sums.
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2. Consider  $f(x) = 8x - x^2$  on the interval  $[0, 8]$ . Let  $n = 8$ .

- (a) Sketch the graph of  $f(x)$ . Divide  $[0, 8]$  into  $n = 8$  subintervals and indicate the endpoints on your graph.
  - (b) Draw the rectangles corresponding to the left and right Riemann sums.
  - (c) Compute the left and right Riemann sums.
  - (d) Compute the indefinite integral  $F(x) = \int f(x) dx$ . What is  $F(8) - F(0)$ ? Make an observation.
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3. Write antiderivatives for each of the following functions:

(a)  $5x^4 - 6x^3 + 2x - 1$

(b)  $\sin(x) + \sec(x) \tan(x)$

(c)  $\frac{1}{8 + 8x^2}$

(d)  $\frac{1}{\sqrt{9 - x^2}}$