

1. For each of the following integrals, identify whether it is a definite integral or indefinite integral, then compute it. (*Hint: geometry*).

$$(a) \int_0^1 2x \, dx \quad (b) \int \sec^2(2x) \, dx \quad (c) \int_{-1}^1 |x| \, dx$$

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2. Let

$$f(x) = \frac{\pi^2}{\sin^2(\pi x)}.$$

Compute  $f'(x)$  and  $f''(x)$ .

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3. Compute the following indefinite integrals:

$$(a) \int (x^{1/2} - 3x^{4/3}) \, dx \quad (b) \int (2 \sin(y) + e^{3y}) \, dy \quad (c) \int (s^3 - \sin(p) + 4qp) \, dq$$

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4. Estimate the value of

$$\int_0^{3\pi/2} (\sin(x) + 1) \, dx$$

using left and right Riemann sums. Use  $n = 6$  intervals.

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5. Compute, without using the fundamental theorem of calculus,

$$\int_0^3 \sqrt{9 - x^2} \, dx.$$