

MATH 215, FALL 2018 (WHYTE) REVIEW PROBLEMS

- (1) Show that $n = 3$ is the only natural number with $n^2 > 2^n$
- (2) Show that if $f : A \rightarrow B$ and $g : B \rightarrow C$ are bijective functions then $g \circ f$ is bijective.
- (3) If a and b are relatively prime then there is an $n \in \mathbb{N}$ such that $a^n \equiv 1 \pmod{b}$
- (4) If $a^2 | b^2$ then $a | b$
- (5) If $f : A \rightarrow B$ is an injective function then for any A_1 and A_2 , subsets of A , $f(A_1 \cap A_2) = f(A_1) \cap f(A_2)$
- (6) If $\gcd(n_1, n_2) = 1$ then for any r_1 and r_2 there is an a with $a \equiv r_1 \pmod{n_1}$ and $a \equiv r_2 \pmod{n_2}$
- (7) If n is prime then n does not divide $(n - 1)!$
- (8) For every $n \in \mathbb{N}$ the sum of the odd numbers less than $2n$ is equal to n^2

The converses of all of (2) through (6) are true, and the converse of (7) is true except for $n = 4$. Can you formulate these statements? Can you prove them?