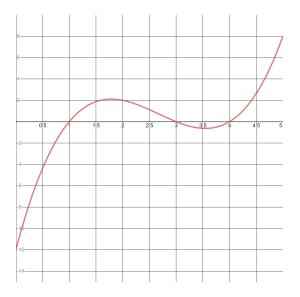
## WORKSHEET 22

## RIEMANN SUMS

28 January 2020

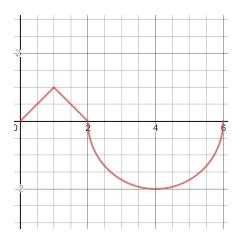
1. (**Review**) Determine where the function  $f(x) = \frac{x^2 - 9}{2x^2 - 10x + 12}$  is discontinuous.

- 2. (Review) Use the Intermediate Value Theorem to show that  $25 8x^2 x^3 = 0$  has a solution in the interval [-2, 4].
- 3. (Warm-up) What is the definition of a Riemann sum for a function f(x) on an interval [a, b]? What are Riemann sums useful for?
- 4. (Warm-up) Sketch the graph of  $f(x) = x^2$  on the interval [0,5]. Draw the left endpoint approximation for the area under the graph with 5 subintervals, and calculate the left Riemann sum that corresponds to the rectangles. Is this an over or under estimate?
- 5. Consider the function  $f(x) = x^3 8x^2 + 19x 12 = (x-1)(x-3)(x-4)$  on the interval [0,5] (the graph is shown below)



- (a) Sketch the midpoint approximation for f(x) using 5 subintervals.
  (b) Calculate the left wight and midmoint Pie.
- (b) Calculate the left, right, and midpoint Riemann sums for f(x) on [0, 5] using 5 subintervals.

6. Consider the following graph of a function g:



By examining the graph, compute the following:

(a) 
$$\int_{0}^{2} g(x) dx$$
  
(b) 
$$\int_{2}^{6} g(x) dx$$
  
(c) 
$$\int_{0}^{6} g(x) dx$$