

# The Algorithm for Finding the $k^{\text{th}}$ Smallest in Expected Linear Time (Non-Recursive)

Let  $T$  be the type of the elements in array  $a$ . As the algorithm runs, at all times the  $k^{\text{th}}$  smallest element of  $a$  lies between positions  $left$  and  $right$ , inclusive. The algorithm terminates when  $left == right$ , at which time both must equal  $k$ .

```
T select( T[] a, Integer k)
    left = 1;
    right = a.length;
    while ( left < right )
        q = partition( a, left, right );
        if ( k < q )
            right = q - 1;
        else if ( k > q )
            left = q + 1;
        else
            left = right = q;
    return a[q];
```

# A Recursive Implementation of The Algorithm for Finding the $k^{\text{th}}$ Smallest in Expected Linear Time

The recursive version of *select()* below is initiated by invoking *select( a, k, 1, a.length)*. It assumes the array *a* is passed by reference and the integer arguments by value, as in C, C++, or Java.

When *select(a, k, left, right)* is called, the  $k^{\text{th}}$  smallest element of the entire array *a* must lie between positions *left* and *right*, inclusive. *select()* completes the computation of the  $k^{\text{th}}$  smallest element and returns it.

```
T select( T[] a, Integer k, Integer left, Integer right)
    if ( left < right )
        q = partition( a, left, right);
        if ( k < q )
            return select( a, k, left, q - 1);
        else if ( k > q )
            return select( a, k, q + 1, right);
        else
            return a[q];
    else
        return a[left];
```