

# Math 180 Practice Exam 2

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Name

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1) Air is being pumped into a spherical balloon at a rate of  $5 \text{ cm}^3/\text{min}$ . Determine the rate at which the radius of the balloon is increasing when the diameter of the balloon is 20 cm

2) Given a function  $f(x) = \sqrt{x}$ , find an approximation of  $\int_0^4 f(x)dx$  using:

- left Riemann sums, splitting the interval into 4 pieces.

- right Riemann sums, splitting the interval into 4 pieces.

3) A piece of wire of length 50 cm is cut into two pieces. One piece is shaped into a circle and the other is shaped into a square. Where should the wire be cut to minimize the sum of the area of the two shapes?

4) Given vectors  $u = \langle 1, 4 \rangle$ ,  $v = \langle -3, 6 \rangle$  and  $w = \langle -8, 2 \rangle$  compute/find:

- $u \cdot v$

- $v \cdot w$

- Which pairs of vectors are orthogonal?

- $\text{proj}_u(v)$

- $\text{proj}_u(w)$

5) Given  $f(x) = 2x^3 - 9x^2 - 108x + 2$  determine **a)** the intervals of increase/decrease, **b)** the intervals upon which  $f$  is concave up/down, **c)** local mins/maxes, and **d)** the inflection points.