The Dihedral Group $D_3$

The dihedral group $D_3$ is obtained by composing the six symmetries of an equilateral triangle.

There are three rotations

There are three reflections.

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