

**Math 435 Number Theory I**  
Problem Set 2

**Due: Friday September 9:** Do 3 of the following problems.

All work should be shown. Proofs should be written clearly in complete sentences.

Important Dates

Midterm 1: Friday September 30

Midterm 2: Friday November 11

Final Exam: Friday December 9, 8:00 am

1) Suppose  $\gcd(a, b) = 1$ ,  $a|c$  and  $b|c$ . Give two proofs that  $ab|c$ , one using the Fundamental Theorem of Arithmetic and one not.

2) Find a positive integer  $n$  such that  $n/2$  is a square,  $n/3$  is a cube and  $n/5$  is a fifth power.

3) It is unknown if there are infinitely many primes  $p$  such that  $p$  and  $p + 2$  are prime. Prove that 3 is the only prime such that  $p$ ,  $p + 2$  and  $p + 4$  are prime.

4) (Programming Project) Write a computer program which when given positive integers  $a, b, c$  will decide if the equation  $aX + bY = c$  has a solution and will find a solution if there is one. Use the program to find a solution to each of the equations:

$$171X + 311Y = 1$$

$$572470376X + 597730781Y = 4536266$$