## Stat/Econ 473 Game Theory Problem Set 7

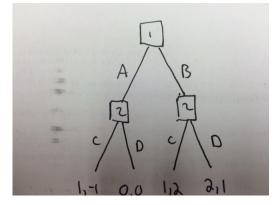
## Due: Thursday March 10

From the Text: Do problems: 14.10, 14.11-14.13

**Comments** a) For 14.10 you may use your analysis from 4.8)-4.11 on problem set 2 and 5.7–5.9 problem set 3.

b) For Problem 14.13) just give an example of a subgame perfect equilibrium where (U,R,E) is played in the first game.

1) Consider the following extensive game.



Let  $\sigma$  be a mixed strategy for Player 2 where Player 2 uses CC with probability .3, CD with probability .1, DC with probability .4 and DD with probability .2.

a) Find an equivalent behavioral strategy  $\tau$ . Under  $\tau$  what is the probability Player 2 plays C if Player 1 plays A. Under  $\tau$  what is the probability Player 2 plays C if Player 1 plays B.

b) Show that  $v_2(A, \sigma) = v_2(A, \tau)$  and  $v_2(B, \sigma) = v_2(B, \tau)$ .

c) Let  $\hat{\tau}$  be the behavioral strategy where: i) if Player 1 plays A, then Player 2 plays C with probability .5 and ii) if Player 1 plays B, then Player 2 plays C with probability .7. Find an equivalent mixed strategy  $\hat{\sigma}$ .

2) We play the following game twice.

	L	С	R
Т	$10,\!10$	$2,\!12$	$0,\!13$
Μ	12,2	$^{5,5}$	$0,\!0$
В	13,0	$0,\!0$	$1,\!1$

a) In the extensive form of the repeated game how many subgames are there (not counting the full game)? .

b) Describe pure strategies  $\sigma$  for Player 1 and  $\tau$  for Player 2, such that  $(\sigma, \tau)$  is a subgame perfect equilibrium and both Players make the same move in the second game that they made in the first game. How many such equilibria are there?

c) Let  $\hat{\sigma}$  be the strategy of Player 1-play T in the first game and if the outcome of the first game is (T,L) play M in the second game, otherwise play B. Let  $\hat{\tau}$  be the strategy for Player 2-play L in the first game, if the outcome of the first game is (T,L) play C in the second game otherwise play R. Argue that  $(\hat{\sigma}, \hat{\tau})$  is a subgame perfect equilibrium.

d) Is there a subgame perfect equilibrium where (T,L) is played in the second game?