

Quiz 6

MATH 210, CALCULUS III, SUMMER 2015

NAME:

Problem 1. Find an equation of the line of intersection of the planes Q and R where

$$Q: -x + 2y + z = 1 \quad n_Q = \langle -1, 2, 1 \rangle$$

$$R: x + y + z = 0 \quad n_R = \langle 1, 1, 1 \rangle$$

$$z = 0:$$

$$-x + 2y = 1 \rightarrow x = 2y - 1$$

$$x + y = 0$$

$$2y - 1 + y = 0$$

$$3y = 1$$

$$y = \frac{1}{3}$$

$$x = \frac{2}{3} - 1 = -\frac{1}{3}$$

$$\text{Point: } \left(-\frac{1}{3}, \frac{1}{3}, 0\right)$$

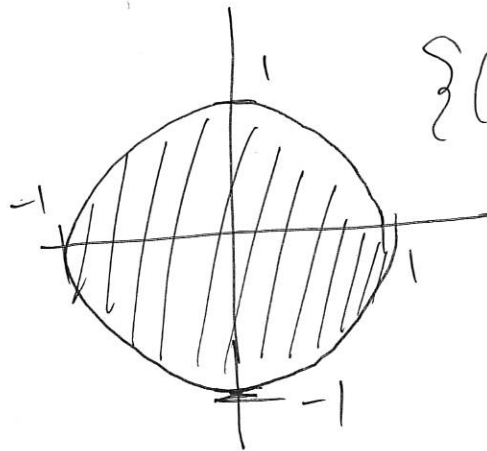
$$\begin{vmatrix} \bar{i} & \bar{j} & \bar{k} \\ -1 & 2 & 1 \\ 1 & 1 & 1 \end{vmatrix} = \bar{i}(2-1) - \bar{j}(-1-1) + \bar{k}(-1-2) = \langle 1, 2, -3 \rangle$$

$$r(t) = \left\langle -\frac{1}{3}, \frac{1}{3}, 0 \right\rangle + t \langle 1, 2, -3 \rangle = \left\langle -\frac{1}{3} + t, \frac{1}{3} + 2t, -3t \right\rangle$$

Problem 2. Find and sketch the domain of the function $g(x, y) = \sqrt{1 - x^2 - y^2}$.

$$1 - x^2 - y^2 \geq 0$$

$$1 \geq x^2 + y^2$$



$$\{(x, y) : x^2 + y^2 \leq 1\}$$