- 1. Exercise 3.4 in the text.
- 2. Exercise 3.8 in the text.
- 3. Exercise 3.34 in the text.
- 4. Exercise 4.5 in the text, and show your work.
- 5. Exercise 4.36 in the text.
- 6. Consider a probability distribution on the numbers 0, 1, 2, ..., 20 with probabilities given by $P(k) = a(\frac{1}{2})^k$.

a) Find a so that the sum of all probabilities is 1, and hence P(k) is a legitimate formula for a probability distribution.

b) Let X be a random variable with the above probability distribution. Calculate the expected value and the variance of X. Hint: It's not so nice to do this by hand. Here's a function in **R** for computing the expected value:

```
expected.value = function(){
```

```
a = 1
s = 0
for(k in 0:20){
s = s + k*a*((1/2)^k)
}
return(s)
```

}

All you need to do to use this is change the value of a from a = 1 to what you got in part a), run this code in R and then run the command **expected.value()** to run the function. Here's another hint: you can modify this function to get the expected value of X^2 and then use the results to compute the variance of X.

c) Here is an R function to generate (pseudo-)random samples of size n from this distribution:

```
p_k = function(k){
```

a = 1
value = a*((1/2)^k)
return(value)

```
}
```

```
my.sample = function(n){
p = p_k(0:20)
s = sample.int(21, size = n, replace = TRUE, prob = p)-1
return(s)
}
```

To use this, first change the value of a in the p_k function from a = 1 to the value you got in part a). Then run the two functions in R. Finally,

to get a sample of size n from the distribution, run my.sample(n) or samp = my.sample(n) in order to store a sample of size n into the variable samp. Compute the sample mean and sample variance of a sample generated from my.sample using values of n = 10, 50, 100, 500, 1000 (remember you can use R functions mean(samp) and var(samp)). How do the values compare to the values you got in part b) for population mean and variance? Print all your results from the R console.