# Marginal Analysis-simple example Math165: Business Calculus 

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Spring 2010, Week4 Lec3

## Marginal Analysis

## Given:

- cost per unit: $\mathbf{c}=\$ 6$ per unit, cost to producer
- Demand Relation: $q=100-2 p$,
- production level: q,
- price per unit: p, selling price


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 example part 1Find:

- $\mathbf{C}(\mathbf{q})$, Cost function
- $R(q)$, Revenue function
- $\mathbf{P ( q )}$, Profit function
- $\mathbf{q}_{\text {max }}$ production level to maximize profit
- $\mathrm{P}_{\text {max }}$ the price to charge for each unit to maximize profit
- maximum profit $\mathbf{P}_{\text {max }}$
- $\mathrm{C}_{\text {avg }}=\frac{\mathrm{C}(\mathrm{q})}{\mathrm{q}}$ Average Cost function
- break even point(s), set $P(q)=0$ and solve for $q$


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 example part 1- There are two standard ways to approach the problem of finding $\mathbf{q}_{\text {max }}$
1st solve $M R=M C$ i.e. set $R^{\prime}(q)=C^{\prime}(q)$ and solve for $q_{\text {max }}$
Using this method you never need to actually find the profit
function. Sometimes this is useful.



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- This should be obvious from the graph:



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Cost Function

Cost Function:

- cost $=$ fixed cost + variable cost
- for this problem assume fixed cost is zero.
- variable cost $=$ cost per unit times number of units
- $C(q)=6 q$, Cost Function


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Revenue Function

- Revenue $=($ income from each unit sold $) \cdot($ number units sold $)$
- $R(q, p)=p \cdot q$,
- Use the demand relation to convert $\mathbf{p}$ to a function of $\mathbf{q}$,
- Demand Relation: $\mathbf{q}=100-2 p$
- solve for p as a function of q


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q & =100-2 p  \tag{1}\\
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- This gives the demand relation in the form $\mathbf{D}(\mathbf{q})=50-\frac{1}{2} \cdot \mathbf{q}$
- $R(q)=\left(50-\frac{1}{2} q\right) q=50 q-\frac{1}{2} q^{2}$, Revenue Function


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## Profit:

- $P(q)=R(q)-C(q)$
- $P(q)=\left(50 q-\frac{1}{2} q^{2}\right)-(6 q)$
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- solve MP $=0$
- solve $\mathbf{P}^{\prime}=44-q=0$
- gives $\mathbf{q}_{\text {max }}=44$ units.


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- gives $\mathbf{q}_{\max }=44$ units. This is the quantity that must be made and sold to maximize profit.
- use the demand relation to find $\mathbf{p}_{\max }$. (any form will do).
- $\mathrm{p}_{\max }=50-\frac{1}{2} \cdot 44=\$ 28$ per unit.


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- $C(q)=6 q$
- $R(q)=50 q-\frac{1}{2} q^{2}$
- $M C=C^{\prime}(q)=6$
- $M R=R^{\prime}(q)=50-q$
- solve MR) $=$ MC
- solve $\mathbf{R}^{\prime}(\mathbf{q})=C^{\prime}(q)$
- solve $50-\mathrm{q}=6$
- gives $\mathrm{q}_{\max }=44$
- $P_{\max }=R\left(q_{\max }\right)-C\left(q_{\max }\right)=50(44)-\frac{1}{2}(44)^{2}=\$ 968.00$
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## Marginal Analysis

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- solve MR) $=$ MC
- solve $\mathbf{R}^{\prime}(\mathbf{q})=\mathbf{C}^{\prime}(\mathbf{q})$
- solve $\mathbf{5 0} \mathbf{- q}=\mathbf{6}$
- gives $\mathbf{q}_{\max }=44$
- $P_{\text {max }}=R\left(q_{\max }\right)-C\left(q_{\max }\right)=50(44)-\frac{1}{2}(44)_{\Lambda}^{v}=\$ 968.00$
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- solve MR) $=$ MC
- solve $\mathbf{R}^{\prime}(\mathbf{q})=\mathbf{C}^{\prime}(\mathbf{q})$
- solve $\mathbf{5 0} \mathbf{- q}=\mathbf{6}$
- gives $\mathbf{q}_{\max }=44$
- $P_{\max }=R\left(q_{\max }\right)-C\left(q_{\max }\right)=50(44)-\frac{1}{2}(44)_{\Lambda}^{26}=\$ 968.00$
- This was easier and there was no need to find the profit function $\mathbf{P}(\mathbf{q})$.

