## Instruction

The midterm consists of 3 problems, each worth 34 points (The maximal grade is 100). For this you will have 45 minutes during class. The identities file will be appended to the exam and no other material is allowed. The answers to the problems should be answered in the designated areas.

## Problems

Problem 1. For each of the following statements determine if it is true are false. No explanation required, circle the correct answer:
a. $1 \in\{-1,2,\{1,1\},\{\{1\}\}\}$. True $\backslash$ False
b. $13 \in\left\{n^{2}+n+1 \mid n \in \mathbb{N}_{\text {even }}\right\}$. True $\backslash$ False
c. $6 \in\left\{n \in \mathbb{N} \mid\left\{m \in \mathbb{Z} \mid m^{2}+n \leq 5\right\}=\emptyset\right\}$. True $\backslash$ False

## Math 300-Midterm 1

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(Instructor: Tom Benhamou)
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Problem 2. Prove that for all positive integers $a, b$, if both $2 a+b$ and $a-2 b$ are divisible by 3 then $a$ is divisible by 3 .

## Solution:

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Problem 3. Let $\alpha$ be the statement:

$$
\forall x \in \mathbb{N} \cdot\left(\exists y \in \mathbb{N} .\left((y<x) \vee\left(y^{2}<x^{2}\right)\right)\right)
$$

a. Present $\neg \alpha$ without the " $\neg$ " symbol. No explanation required.

## Solution:

$\neg \alpha \equiv$
b. Prove or disprove $\alpha$.
solution:

