Planes, Vectors and Automobiles

- 1. Given a vector $\vec{v} = (a, b)$ the formulas for the following
- (a) A unit vector parallel to \vec{v}
- (b) A vector perpendicular to \vec{v}
- (c) The magnitude of \vec{v}

2. Without looking at notes, write the geometric equations for dot product and cross product.

3. True or False: Is $(\vec{v} \times \vec{u}) \times \vec{w} = \vec{v} \times (\vec{u} \times \vec{w})$. If true, prove, if false, give a counter example.

4. Write an equation of the plane with normal vector n passing through the given point

(a)
$$n = \langle 1, 3, 2 \rangle, (4, -1, 1)$$

(b)
$$n = i, (3, 1, -9)$$

5. Find an equation of the plane passing through the three points

- (a) (1,2,3), (3,2,1), (2,1,3)
- (a) (0,0,0), (1,0,0), (2,0,0)

6. Find the intersection of the line and plane

(a)
$$x + y + z = 14, r(t) = \langle 1, 1, 0 \rangle + t \langle 0, 2, 4 \rangle$$

- **(b)** $z = 12, r(t) = t \langle -6, 9, 36 \rangle$
- 7. Compute the angle between the two planes
- (a) 2x + 3y + 7z = 2 and 4x 2y + 2z = 4
- (b) The plane through (1, 0, 0), (0, 1, 0), (0, 0, 1) and the y-plane