## Worksheet # 7

MATH 294 ESP Workshop Spring 2016 See the attached paper Recounting the rationals by Calkin and Wilf.

**Problem 1.** Fill in the next row of the tree in figure 1.

**Problem 2.** Prove *The numerator and denominator at each vertex are relatively prime.* 

**Problem 3.** Prove *Every reduced positive rational number occurs at some vertex.* 

**Problem 4.** Prove No reduced positive rational number occurs at more than one vertex.