

2.2 Separable Equation

1. Solve the equation $\frac{dx}{dt} = \frac{t}{xe^{t+2x}}$

2. Solve the initial value problem

(a) $\frac{1}{2} \frac{dy}{dx} = \sqrt{y+1} \cos x, \quad y(\pi) = 0$

(b) $x^2 dx + 2y dy = 0, \quad y(0) = 2$

2.3 Linear Equation

1. Solve the equation

(a) $\frac{dy}{dx} = x^2 e^{-4x} - 4y$

(b) $x \frac{dy}{dx} + 3(y + x^2) = \frac{1}{x}$

2. Solve the initial value problem

$$\sin x \frac{dy}{dx} + y \cos x = x \sin x, \quad y\left(\frac{\pi}{2}\right) = 2$$