Math 170: Quiz 5

Sayan Mukherjee's discussion

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Problem 1. Find the following limit, with proof:

$$\lim_{x \to 3} \frac{\sqrt{x+1}-2}{x-3}.$$

Solution.

$$\lim_{x \to 3} \frac{\sqrt{x+1}-2}{x-3} = \lim_{x \to 3} \frac{(\sqrt{x+1}-2)(\sqrt{x+1}+2)}{(x-3)(\sqrt{x+1}+2)} = \lim_{x \to 3} \frac{(x+1)-4}{(x-3)(\sqrt{x+1}+2)} = \frac{1}{4}.$$

Rubric.

- $\bullet~+2\mathrm{pts}$ for multiplying numerator and denominator with the conjugate
- +2pts for simplifying the fraction to $\frac{1}{\sqrt{x+1+2}}$, ie cancelling (x-3) off the numerator and denominator
- +1pt for correct answer $(\frac{1}{4})$