

5. (a) How many years for \$1,000 to grow to \$1,000,000 if compounded quarterly?
Compounded quarterly at 10%/year.

$$r = 10\% = .10$$

$$n = 4$$

$$F = P \left(1 + \frac{r}{n} \right)^{nt}$$

$$1,000,000 = 1,000 \left(1 + \frac{.1}{4} \right)^{4t}$$

$$1000 = (1 + .025)^{4t}$$

$$1000 = (1.025)^{4t}$$

$$\ln 1000 = \ln [(1.025)^{4t}]$$

$$\ln 10^3 = 4t \cdot \ln(1.025)$$

$$3 \ln 10 = 4t \ln(1.025)$$

$$t = \frac{3}{4} \cdot \frac{\ln(10)}{\ln(1.025)}$$

$$t \approx 69.9 \text{ years}$$

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